



GUÍA 3: INTEGRACIÓN TRIGONOMÉTRICA

Calcule las siguientes integrales trigonométricas.

$$1. \int \tan^5(x) \sec^2(x) dx$$

$$7. \int \sen^3(x) \cos^2(x) dx$$

$$2. \int \sen^2(x) \cos^2(x) dx$$

$$8. \int \sen^2(\pi x) \cos^5(\pi x) dx$$

$$3. \int \sec^2(x) \tan(x) dx$$

$$9. \int \frac{\sen^3(\sqrt{x})}{\sqrt{x}} dx$$

$$4. \int \sen^4(x) dx$$

$$10. \int (1 + \cos^2(\theta))^2 d\theta$$

$$5. \int \tan^2(x) dx$$

$$11. \int \frac{\cos^5(\alpha)}{\sqrt{\sen(\alpha)}} d\alpha$$

$$6. \int \cos^5(x) dx$$

$$12. \int \cos(\theta) \cos^5(\sen(\theta)) d\theta$$

Calcule las siguientes integrales usando la sustitución trigonométrica sugerida.

$$1. \int \frac{1}{x^2 \sqrt{x^2 - 9}} dx, \quad x = 3 \sec(\theta)$$

$$3. \int \frac{x^3}{\sqrt{x^2 + 9}} dx, \quad x = 3 \tan(\theta)$$

$$2. \int x^3 \sqrt{9 - x^2} dx, \quad x = 3 \sen(\theta)$$

$$4. \int \frac{1}{\sqrt{x^2 - 49}} dx, \quad x = 7 \sec(\theta)$$

Calcule las siguientes integrales usando la sustitución más conveniente.

$$1. \int \frac{1}{x^2\sqrt{25-x^2}} dx$$

$$4. \int \frac{\sqrt{x^2-9}}{x^3} dx$$

$$2. \int \frac{1}{\sqrt{x^2+16}} dx$$

$$5. \int \frac{x}{\sqrt{x^2-7}} dx$$

$$3. \int \sqrt{1-4x^2} dx$$

$$6. \int x\sqrt{x^2+4} dx$$

Identidades trigonométricas útiles.

$$\blacksquare \quad \operatorname{sen}^2(x) + \cos^2(x) = 1$$

$$\blacksquare \quad \cos^2(x) = \frac{1 + \cos(2x)}{2}$$

$$\blacksquare \quad \sec^2(x) = 1 + \tan^2(x)$$

$$\blacksquare \quad \frac{d}{dx} \sec(x) = \sec(x) \tan(x)$$

$$\blacksquare \quad \operatorname{sen}^2(x) = \frac{1 - \cos(2x)}{2}$$

$$\blacksquare \quad \frac{d}{dx} \tan(x) = \sec^2(x)$$

$$\blacksquare \quad \int \tan(x) dx = \ln |\sec(x)| + C$$

$$\blacksquare \quad \int \sec(x) dx = \ln |\sec(x) + \tan(x)| + C$$

$$\blacksquare \quad \operatorname{sen}(x) \cos(y) = \frac{1}{2} (\operatorname{sen}(x-y) + \operatorname{sen}(x+y))$$

$$\blacksquare \quad \operatorname{sen}(x) \operatorname{sen}(y) = \frac{1}{2} (\cos(x-y) - \cos(x+y))$$

$$\blacksquare \quad \cos(x) \cos(y) = \frac{1}{2} (\cos(x-y) + \cos(x+y))$$