Estimating Learning-by-Doing in the Personal Computer Processor Industry^{*}

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Abstract

I estimate a dynamic cost function involving Learning-by-doing in the Personal Computer Processor industry. Learning-by-doing is an important characteristic of semiconductor manufacturing, but no previous empirical study of learning in the processor market exists. Using a new econometric method, I estimate parameters of a cost function under a Markov perfect equilibrium. I find learning rates between 2.54% and 24.86%, and higher production costs for AMD compared to INTEL, the two firms in the market. Around 12% of the differences in costs between firms is explained by the lower learning that AMD obtains given its lower production levels. These learning rates are lower than those of other semiconductors products and they indicate that when the firms begin the production in the fabs they have already advanced in their learning curve and most of the learning occurs *before-doing* in the development facilities.

^{*}This paper is a draft of the third chapter of my dissertation. In the first chapter I estimate a random coefficient model of demand and analyze the importance of the Intel brand in demand for CPU. In the second chapter I analyze different measures of market power in a dynamic model of firm behavior. Please do not cite or circulate. All comments are welcome.

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1 Introduction.

The Central Processing Unit (CPU) is the brain of the personal computer (PC), performs all of the information processing tasks required for computing. The technological development of the CPU, the most important PC component, has been one of the keys to growth in the PC industry over the last three decades. Two of the clearest trends in the CPU and the PC markets are the sustained increase in product quality and a steep decrease in price over time. Several reasons have been cited for these trends, the most important of which are strategic interactions between firms, a continuous introduction of new, improved products, and the existence of learning-by-doing in the production process.

The evidence for learning-by-doing in the semiconductor industry is abundant. It has been well documented that learning plays an important role in the semiconductor industry due to significant reductions in failure rates. When a new product is introduced, the proportion of units that passes quality and performance tests (*yield*) could be as low as 10% of the output. Production experience and adjustment in the process over time decrease failure rates, increasing yields up to 90%, which reduces unitary production costs over the lifetime of a product (Irwin and Klenow, 1994). The empirical applications of learning in the semiconductor industry have concentrated on memory manufacturing (Baldwin and Krugman 1988; Dick 1991; Irwin and Klenow 1994; Gruber, 1996, 1999; Hatch and Mowery, 1999; Cabral and Leiblein, 2001; Macher and Mowery, 2003; Siebert, 2008), and even though memory and CPU production processes are subject to the same type of learning economies, no evidence exists of the importance of learning in CPU manufacturing. Surprisingly, while most of the studies in the PC CPU industry recognize the existence of learning in the manufacturing process, they have focused on other characteristics of the market and ignored cost determinants and learning-by-doing as a key component of the industry (Aizcorbe 2005, 2006; Gordon 2008; Song 2006, 2007).

In this paper I estimate the extent of learning-by-doing in the PC CPU industry using a new econometric method by Bajari, Benkard and Levin (2007). Compared to previous emprirical studies of learning-by-doing, this method requires weaker assumptions regarding firms dynamic behavior. The method employs a closed loop approach, which allows me to control for how the firms think their rivals will react in the future to changes in their current behavior. Additionally, the method has several computational advantages because it makes use of simulations that (1) do not require neither to find an algebraic solution for the equilibrium of the game, and (2) do not require me to choose amongst possible multiple equilibria. Instead, the method assumes that the observed behavior is the equilibrium that firms decide to play. This method makes it feasible to estimate learning rates while controlling for strategic interactions among firms, heterogeneous preferences of consumers, and periodic introduction of new, differentiated products, into the market. I use a proprietary dataset from In-Stat/MDR, a research company specializing in the CPU Industry that is the data source for all the analysis and forecasting done in the PC CPU market. It contains detailed quarterly shipment estimates and prices for 29 products by AMD and INTEL over 48 time periods from 1993 to 2004.

The analysis in this paper differs from the previous literature in several ways. Most previous studies have assumed that products are homogeneous and that firms are symmetric; in most cases, they have also taken demand elasticity as a parametric assumption (one exception is Siebert, 2008). In this paper I use estimates from a random coefficient demand model (Salgado, 2008) which allows me to control for the existence of differentiated products and for heterogeneity of preferences among consumers. This also makes it possible to analyze strategic interactions among firms in a complicated game in which firms choose prices for each of their available differentiated products under dynamics given by learning-by-doing.

The results show that there are large differences between firms' estimated production costs, with AMD's average costs more than twice Intel's average costs. These differences are explained by both a higher production cost upon introduction of a product and a lower learning gain due to lower production. The average estimated learning rates fluctuate between 2.54% and 17.01% for AMD and between 4.74% and 24.86% for Intel, which are lower than those found in other empirical studies of semiconductor products, which have found average learning rates of 20%. This difference in learning rates suggests that in the CPU market, firms transfer the production process from the development facilities to the production fabs succesfully once they have already advanced in their learning curve.

The structure of the paper is as follows. Section 2 reviews the most relevant studies, both theoretical and empirical, in the learning-by-doing literature. Section 3 describes a structural model that captures the characteristics of the market I am interested in analyzing. Section 4 presents the econometric method and explain how can it be applied to estimate the rates of learning in CPU manufacturing. Section 5 presents the results and the findings and section 6 concludes.

2 Literature Review

The learning-by-doing hypothesis states that in some manufacturing processes, cost are reduced as firms gain production experience. This hypothesis originated with Wright (1936), who observed that direct labor costs of airframe manufacturing fell by 20% with every doubling of cumulative output. Since then, many empirical studies have analyzed the existence of learningby-doing in a variety of industrial settings, and a number of theoretical papers have analyzed different implications of learning for endogenous growth, market concentration, and firms' strategic interactions (Lee 1975, Spence 1981, Gilbert and Harris 1981, Fudenberg and Tirole 1983, Ghemawat and Spence 1985, Ross 1986, Dasgupta and Stiglitz 1988, Mookherjee and Ray 1991,Habermeier 1992, Cabral and Riordan 1994, Cabral and Leiblein 2001).

Theoretical analyses have shown that learning-by-doing could create entry barriers and strategic advantages for existing firms (Lee 1975, Spence 1981, Ghemawat and Spence 1985, Ross 1986, Gilbert and Harris 1981) and facilitate oligopoly collusion (Mookherjee and Ray, 1991). Gruber (1992) presents a model in which learning-by-doing could generate stability in market share patterns over a sequence of product innovations, given the existence of leaders and followers in the market. Cabral and Riordan (1994) show that learning-by-doing creates equilibria with increasing dominance of one firm in the market and might generate predatory pricing behavior by the leaders who use their cost advantage to prevent new firms from entering the market. Besanko, et.al. (2007) analyze a model of learning-by-doing to explain the incentives that firms have to price strategically, showing that firms might price more aggressively in order to learn more quickly and gain dominance over competitors, as well as to prevent their competitors from learning.

The existence of learning-by-doing in the semiconductor manufacturing process has been widely analyzed. The source of learning has been attributed to the adjustments that are necessary to obtain high productivity during fabrication. The semiconductor production process is based on hundreds of steps in which circuit patterns from photomasks are imprinted in silicon wafers and then washed and baked in several layers, thus forming the millions of transistors that allow the chip to function as an information processing device. These steps must be performed under precise environmental conditions that are controlled and adjusted continuously. When a product is first transfered from the development labs to full production in the fabs, the number of units that pass control quality tests (yield) is very small, and several fine-tuning steps need to be taken in order to obtain high yields. Given that the production cost of a wafer is independent of the number of working chips at the end of the product line, low yields mean higher production cost per working unit. It is the increase in the yield rates that generates reduction in the production cost of the final products. Hatch and Mowery (1998) analyze detailed production data on unitary yields for a number of semiconductor chips and conclude that both cumulative production and engineering analysis of the production output are the sources of improvements in yield rates

over the lifetime of the products.

The most common specification in the empirical analysis of learning-bydoing is based on a constant learning-elasticity

$$\log c_t = \alpha + \eta \log E_{t-1} + \varepsilon_t \tag{1}$$

Where c_t represents unitary production costs, usually assumed constant within a period, and E_{t-1} reflects some measure of production experience, usually proxied by cumulative production. Using this specification, the goal of the empirical analysis is to estimate the constant experience-elasticity η and use it to measure a *learning rate*, which measures the percentage reduction in average cost when cumulative production doubles, defined by:

$$r_t \equiv \frac{c(E_t) - c(2E_t)}{c(E_t)} = 1 - 2^{\eta}$$
(2)

In a seminal empirical paper on learning-by-doing in the semiconductor industry, Irwin and Klenow (1994) construct a structural model of learningby-doing and estimate learning spillovers among seven generations of DRAM¹. They focus the analysis on estimating how the cumulative production of each product, as well as the cumulative production of all other products, affects unitary average costs. Using quarterly data from 1974 to 1992, they find average learning rates of 20% for the different products. They also find that firms learn three times more from internal cumulative production than from spillovers from other firms experience and that cumulative production of

¹Dynamic Random Access Memory, one of the volatile memory devices used in computers.

previous generations has weak effects on the costs of new products. In their model, they assume that products are homogeneous and firms are symmetric, and they solve for the Cournot equilibrium of the dynamic game under an open-loop assumption. This assumption means that firms commit to a path of production over the future in an initial time period and that they do not modify this path in the future. This implies that firms will not adjust their plans over time depending on how the game evolves, nor will they react to changes in their competitors' behavior. If the game under analysis has some random components, as in our application, this assumption is clearly not valid. The authors estimate the parameters of the cost function with a GMM method using instruments and the first order conditions of the dynamic problem. They also propose the use of a non-linear least squares (NLLS) method that assumes a functional form for the dynamic $cost^2$, which facilitates the estimation process and avoid the need of valid instruments. Gruber (1998) applies the NLLS method to the production of EPROM³ chips and finds learning rates between 23% and 30%.

More recently, Siebert (2008) explore learning-by-doing recognizing that different generations of products are competitors in the demand side of the market. He estimates a dynamic oligopoly model under a Markov perfect equilibrium, in which firms choose quantities of each available product. He assumes that firms base their decisions only on industry total cumulative production; furthemore, he assumes that products are homogeneous within

 $^{^{2}}$ The dynamic cost is the sum of current period marginal cost and the shadow value of learning

³Erasable Programmable Read-only Memory, one of the memory chips that can keep information even when the source of power is interrupted. They were used as BIOS chips in old PC and other electronics.

a generation, but that sales of other generations have differentiated effects on prices. He also implicitly assumes that the demand function is common across generations of products and assumes a functional form for the dynamic marginal cost. As in Irwin and Klenow (1994), he uses the first order conditions of the dynamic game in a GMM approach to estimate the parameters of the cost function. The author recognizes the externality that production decisions generates over the demand of the other firm' products and find that ignoring this effect generates biased estimates of learning rates. He found learning rates of 34% when taking into account multiproduct effects and 20% when ignoring these effects.

As stated in the introduction, all of the empirical evidence of learningby-doing in the semiconductor industry comes from memory chips manufacturing. This has been mainly because the market in memory chips is more competitive, and market data have been readily available since the 1970s. Based on new data availability for the PC CPU market, a more recent literature has studied different characteristics of the CPU market. Aizcorbe (2005) analyzes a vintage model of new product introduction; Aizcorbe (2006) examines price indices during the 1990s; and Song (2007), Gordon (2008) and Salgado (2008) analyze different models of demand to measure consumer welfare, demand for durable products and the effects of advertising and brand loyalty on demand, respectively. All these papers have ignored the existence of learning-by-doing as a key component of the manufacturing process.

3 The Model

This section presents a structural econometric model that captures the most important characteristics of the PC CPU industry. There are two firms in the market, AMD (A) and INTEL (I), with n_{tA} and n_{tI} products available in period t. Products are differentiated in terms of their quality, which evolves stochastically over time, where quality of product i in period t is given by k_{it} . Products enter and exit the market exogenously to the firms' pricing decision. It is common knowledge that product i enters the market at time t_{i0} and exits the market at time t_{iT} . Firms choose prices for each one of the available products $i \in I_{jt}$ (the set of products available for firm j at time t).

In the remainder of this section, I present details of the three main components of the model: demand, cost functions, and the equilibrium concept of the dynamic game.

3.1 The model of demand

Demand is modeled using a random coefficient model with quality being the only relevant product characteristic. As in Salgado (2008), I use a CPU performance benchmark that measures the speed at which each CPU can complete a number of tasks. Even though a more detailed characterization of the products is possible (using for example clock speed, amount of cache memory, front speed bus and other characteristics) there is a strong correlation between all of these characteristics and the index of performance. I prefer to use a single characteristic to reduce the number of state variables and facilitate the estimation of the dynamic game. Following Nevo (2000), I present the main components of a random coefficient demand model for the CPU industry. We observe the CPU market in t = 1...T time periods. The market has L potential consumers that must decide either buy one of the available products or not. We observe aggregate quantities, prices, and a measure of quality (k_{it}) for each product. The indirect utility of consumer l from choosing product i at time t is given by

$$u_{lit} = \alpha_l (y_l - p_{it}) + \beta_l k_{it} + \xi_{it} + \varepsilon_{lit}$$

$$l = 1 \dots L, i = 1 \dots I_t, t = 1 \dots T$$
(3)

where y_l is the income of consumer l, p_{it} is the price of product i at time t, k_{it} is the measure of quality of product i in time t, ξ_{it} is a product characteristic observed by consumers and firms but unobserved by the researcher, ε_{lit} is a random term with a type I extreme value distribution, α_l is consumer l's marginal utility from income and β_l is consumer l's marginal utility from product quality. Additionally, we assume that the taste coefficients are independent and normally distributed among the population. Under this assumption, the preferences over income and quality of a randomly chosen consumer can be expresed as:

$$\begin{pmatrix} \alpha_l \\ \beta_l \end{pmatrix} = \begin{pmatrix} \alpha + \sigma_{\alpha} v_{\alpha l} \\ \beta + \sigma_{\beta} v_{\beta l} \end{pmatrix}$$
$$v_{\alpha l}, v_{\beta l} \sim N(0, 1)$$

The demand specification also includes an outside good, which captures the preferences of consumers who decide not to buy any of the available products. The indirect utility from this outside good, which is normalized to zero, is:

$$u_{l0t} = \alpha_l y_l + \xi_{0t} + \varepsilon_{l0t} = 0$$

The indirect utility function in (3) can be written as

$$u_{lit} = \alpha_l y_l + \delta_{it}(p_{it}, k_{it}, \xi_{it}; \alpha, \beta) + \mu_{lit}(p_{it}, k_{it}, v_l; \sigma) + \varepsilon_{lit}$$
(4)

$$\delta_{it} \equiv \beta k_{it} - \alpha p_{it} + \xi_{it} \tag{5}$$

$$\mu_{lit} \equiv \sigma_{\alpha} v_{\alpha l} p_{it} + \sigma_{\beta} v_{\beta l} k_{it} \tag{6}$$

where δ_{it} is constant among consumers and is called the mean utility of product *i* at time *t*, and μ_{lit} captures the portion of the utility from product *i* that differs among consumers.

Consumers are assumed to buy one unit of the good that gives them the highest utility. This defines the set of characteristics of consumers that choose good i:

$$A_{it} = \{ (v_l, \varepsilon_{l0t}, \dots, \varepsilon_{lJ_tt}) | u_{lit} \ge u_{lst} \forall s = 0, 1..J_t \}$$

$$\tag{7}$$

The market share for good i in time t correspond to the mass of individuals over the set A_{it} , which can be expressed as

$$s_{it}(k_t, p_t, \delta_t; \sigma) = \int_{A_{it}} dP(v, \varepsilon)$$
(8)

Given the assumption over the distribution of ε , it is possible to integrate

algebraically over ε , so we can rewrite equation (8) as:

$$s_{it}(k_t, p_t, \delta_t; \sigma) = \int \frac{exp(\delta_{it}(p_{it}, k_{it}, \xi_{it}; \alpha, \beta) + \mu_{ijt}(p_{it}, k_{it}, v_l; \sigma))}{1 + \sum_{s=1}^{J_t} exp(\delta_{st}(p_{it}, k_{it}, \xi_{it}; \alpha, \beta) + \mu_{ist}(p_{it}, k_{it}, v_l; \sigma))} dP(v_l)$$

The demand function for a set of parameters $\theta^d = (\alpha, \beta, \sigma_\alpha, \sigma_\beta)$ is given by

$$q_{it}(p_{it}, k_{it}; \theta^d) = s_{it}(k_t, p_t, \delta_t(\alpha, \beta); \sigma_\alpha, \sigma_\beta) M_t$$
(9)

where M_t is the market size at time t.

The estimation of the demand requires to use a GMM method to control for endogeneity of prices. For this, cost determinants like product characteristics that shift the supply but not the demand and that are uncorrelated with product quality (Die Size, Number of Transistors in the chip and production experience) are used. All the details of the estimation are given in Salgado (2008).

3.2 Evolution of quality

The high rate of increase in quality is an important characteristic of the PC CPU market. Product quality increase over time due to the introduction of improvements to existing product and new characteristics that contribute to a higher performance. However, the main determinant of quality evolution in the market is the continuous introduction of new products over time. I model this characteristic of the market as described below.

There is a quality frontier KF(t), which represents the maximum possible quality for a new product and that evolves exogenously over time. New products are introduced into the market at a quality level $(1 - \alpha_n) * KF(t)$, where $\alpha_n \sim \text{Uniform}[\underline{\alpha_n}, \overline{\alpha_n}]$. For old products, there is a probability p_o that the product quality increases in a given period. If the product quality increases, it does so in a proportion α_o , being the new quality $k_t = (1 + \alpha_o)k_{t-1}$, where $\log(\alpha_o) \sim N(\overline{\alpha_o}, \sigma_o)$. Table 1 summarize these processes.

Quality Frontier	KF(t)
Distance from the frontier $(\%)$	$0 < \alpha_n < 1, \alpha_n \text{Uniform}[\alpha_n, \overline{\alpha_n}]$
of a new product	
Probability that an old prod-	p_o
uct increases its quality at time	
t	
Increase in quality $(\%)$ if this	$\alpha_o > 0, \log(\alpha_o) \sim N(\overline{\alpha_o}, \sigma_o)$
is positive	

Table 1: Characteristics of Quality Evolution

It is assumed that both firms know the data generating process that generates the evolution of quality, and that they observe the quality of all the products currently available before making their pricing decisions, they do not know the realization of the random variables α_n , p_o , and α_o for future periods; therefore, when making decisions, they need to take expectations over future realizations of these variables.

3.3 Cost Function

Firms face learning-by-doing in the production process, and therefore the unitary cost decreases with production experience. I assume that learning is given entirely by the cumulative production of each product, and that learning spillovers do not exist.⁴ Individual production cost differs across products depending on two main characteristics: the die size (size of the surface of the chip in the wafer) and the number of transistors in the CPU. The cost function that captures this characteristic of the production process is the following, where i denotes an specific product⁵

$$c_{it} = \theta_{0j}^{c} + \theta_{1}^{c} DS_{i} + \theta_{2}^{c} TR_{i} + \theta_{3}^{c} \log(E_{it}) + \varepsilon_{it}$$
(10)
$$\varepsilon_{it} \sim N(0, \sigma_{\varepsilon}^{2})$$

In this specification I allow the constant term θ_{0j}^c to be firm specific to control for potential differences in production cost between firms, DS_i is the die size and TR_i is the number of transistors in the chip. For higher DS, fewer chips are produced per wafer; the higher TR the more complicated the production process is and therefore the individual cost per chip is higher. These characteristics are fixed for a particular product over its life. Given that I don't have data on production experience in the development facilities before the product is transferred to the fabs, I assume that for all products at the time of their introduction $E_{it_0} = 1$. Hence, the expected cost of production when a product is first introduced is $\theta_{0j}^c + \theta_1^c DS_i + \theta_2^c TR_i$, and it is reduced, at a decreasing rate, with production experience. For this specification of the cost function, the elasticity of production experience and

 $^{^{4}}$ Hatch and Mowery (1999) find that learning could be the result not only of cummulative production, but also of management efforts to analyze production data and discover the sources of failures.

⁵I use a cost function that is linear in parameters to simplify the estimation algorithm. The use of a log-log function, as is usual in the learning-by-doing literature, increases notoriously the computation burden of the algorithm.

the learning rate, defined in equation (2), are given by:

$$\eta_{it} = \frac{\theta_3^c}{c_{it}}$$

$$r_{it} = -\theta_3^c \frac{\log(2)}{c_{it}}$$
(11)

Production experience is given by cumulative production of each product, and its equation of motion is given by

$$E_{it} = \sum_{\tau=t_{i0}}^{t-1} q_{i\tau}$$
$$E_{it+1} = E_{it} + q_{it}$$

3.4 Single Period profit function

The demand and cost functions previously presented define the per-period profit function for firm j as

$$\pi_{jt}(p_{jt}, p_{-jt}, \mathbf{s}_t) = \sum_{i \in I_{jt}} q_{it}(\mathbf{p}_{jt}, \mathbf{p}_{-jt}, \mathbf{k}_t)(p_{it} - c(E_{it}))$$

Where \mathbf{p}_{jt} and \mathbf{p}_{-jt} are the vector of prices for firm j and its competitor (-j), $\mathbf{s}_t = [\mathbf{k}_t, \mathbf{E}_t]$ is the vector of profit-relevant state variables for firm j at time t, which is composed of the vector of quality for all products available in the market at time t (\mathbf{k}_t) and the vector of production experience (\mathbf{E}_t). Notice that the quality of each product in the market enters the demand function of every other product in a non-linear way through the random coefficient demand model, while experience enters only the cost function of the corresponding product.

3.5 The Game and the Equilibrium Concept

In every period firms simultaneously choose the price for each of their available products $i \in I_{jt}$ to maximize

$$\Pi_{jt}(p_{jt}, p_{-jt}, s_t) = E_t [\sum_{\tau=t}^{\infty} \beta^{\tau-t} \pi_{j\tau}(p_{j\tau}, p_{-j\tau}, s_{\tau})]$$
(12)

where the expectation operator is applied over the realization of present and future cost shocks and the evolution of quality for each product.

Following Benkard, Bajari and Levin (2007), I focus the equilibrium analysis on pure strategy Markov perfect equilibria (MPE). In an MPE each firm's equilibrium strategy depends only on the profit-relevant state variables. A Markov strategy is defined as a function $\sigma_j : S \to A_j$ where Srepresents the state space and A_j represents the set of actions for firm j. A Markov strategy profile is a vector $\sigma = (\sigma_j(s), \sigma_{-j}(s))$.

If firms' behavior is given by a Markov strategy profile σ , the maximized payoff function at a given state s can be written as

$$V_j(\mathbf{s};\sigma) = E_t[\sum_{\tau=t}^{\infty} \beta^{\tau-t} \pi_{j\tau}(\sigma_j(s_{\tau}), \sigma_{-j}(s_{\tau}), s_{\tau})]$$
(13)

The strategy profile σ is a Markov Perfect Equilibrium if, given its opponents profile σ_{-j} , each firm does not have any alternative Markov strategy σ'_j that increases the value of the game. This means that σ is an MPE if for all firms j, states s and Markov strategies σ'_j

$$V_j(\mathbf{s};\sigma_j,\sigma_{-j}) \ge V_j(\mathbf{s};\sigma'_j,\sigma_{-j}) \tag{14}$$

The estimation method consist on minimize a loss function based on observations that violate the rationallity constraint (14). The details of this optimization problem are discussed in the next section.

4 Estimation Method

To estimate the model I follow the econometric method of Bajari, Benkard and Levin 2007 (BBL). These authors propose the use of a two-step algorithm to estimate parameters of dynamic models of imperfect competition. In the first stage all parameters that do not involve dynamics are estimated (the demand parameters, the evolution of quality and the policy function); in the second stage, using the estimates of the first stage, the game is simulated into the future to obtain estimates of the value function. Then, the value function estimates are used to estimate the dynamic parameters (cost parameters). In this section I present details of these estimation procedures.

4.1 Demand Function

The demand function is estimated using a random coefficient model of demand (Berry, Levinsohn and Pakes, 1995; Nevo 2000). The relative performance of a product, compared to the fastest available product, is used as a measure of quality, and a dummy for the Intel brand is included to control for the high premium that consumers are willing to pay for Intel products. Cost determinants (die size, number of transistors and production experience) are used as instruments to control for the endogeneity of prices and are employed in a GMM framework to obtain unbiased estimates of the demand function. All estimation details are presented in Salgado (2008).

4.2 The policy function

The policy function reflects the equilibrium behavior of the firms as a function of the state of the game, which can be estimated from the data using the observed prices and the value of the state variables (quality and production experience). The exact functional form of the policy function is the result of the unknown (and possibly multiple) equilibrium of the game. As proposed by BBL, I let the data talk and assume that the observed prices at every state of the game reflects the equilibrium chosen by the firms.

I make two functional form assumptions in order to estimate the policy function. First, I assume that the policy function is quadratic in the observed state variables and linear in the unobserved cost shock. Therefore, it is assumed that the prediction error from a quadratic regression of prices on the observed state variables corresponds to the realization of the cost shocks. These error terms are used to estimate the distribution of the cost shocks , which will in turn be used during the forward simulation of the game. Second, I focus on a subset of the observed state variables. If I consider the profitrelevant state variables to be the quality and experience of all the products available in each period, the dimensionality of the state space changes over time as the number of available products changes. To avoid this problem and to make use of the best possible approximation given the limitations in the size of the dataset, I define three state variables that capture the effects of the main components of the model on the firms' equilibrium pricing decision. The variables considered are:

- The relative quality of each product with respect to the quality frontier (k_{it}) , which affects the demand function.
- The experience of product i (E_{it}), which determines production cost, as previously defined. This variable captures the effect of learning on the pricing decision⁶.
- The total experience of the competitor for its available products $(E_{-jt} = \sum_{k \in I_{-jt}} E_{kt})$. This variable captures the effect on a firm pricing decision when its competitor faces a lower production cost due to learning.

With these three variables I construct a quadratic approximation of the policy function:

$$\hat{p}_{it} = p(k_{it}, E_{it}, E_{-jt}) + \varepsilon_{it} \tag{15}$$

This function is used in the computation of the expected discounted value (EDV) of firms profits using a forward simulation of the game as proposed by BBL.

4.3 Linearization of the value function

The value function is the expected discounted value of firms' profits, evaluated at the equilibrium policy function. Given the assumption that firms use Markov strategies, the value function depends on profit-relevant state variables and not on the history of the game. To obtain an estimate of the value function, I must first compute the EDV of firms profits, taking into account

⁶I could have also included the die size and the number of transistors as state variables, but to simplify the analysis and to concentrate in the effects of learning on pricing, I assume that equilibrium pricing does not depend on these characteristics.

how the firms expect the game to evolve from the current state. The game evolves stochastically over time, due to the random changes in quality of the products, which also affect demand and production experience. Therefore, to compute the EDV of profits, I need to predict the evolution of the game over time. The policy and demand functions were previously estimated so I can use these estimates to predict prices and quantities at any given state of the game. However, I can not predict firms' profits because the parameters of the cost function are unknown. Nevertheless, I can take advantage of the linearity of the cost and profits functions on the unknown cost parameters to predict these linear terms and compute the EDV of them. Here I present how the value function is linearized and how I obtain a prediction of the EDV of these linear terms using a Montecarlo forward simulation of the game. These predictions will be then used to estimate the cost parameters as I describe below.

As presented in equation (4) the value function is given by

$$V_j(\mathbf{s};\sigma,\theta^c) = E_t[\sum_{\tau=t}^{\infty} \beta^{\tau-t} \pi_{j\tau}(\sigma(s_{\tau}), s_{\tau};\theta)]$$

Where $\sigma(s)$ is the policy function representing the equilibrium prices as a function of the state of the game. For notation simplicity, let p_{it}^* be the equilibrium price of product *i* at time *t* (given the observed value of the state variables) and let \mathbf{p}_{τ}^* and \mathbf{k}_{τ}^* be the vectors of prices and quality of all the products available at time τ . Then we can rewrite the value function as

$$V_j(\mathbf{s}_t; \sigma, \theta) = E_t \left[\sum_{\tau=t}^{\infty} \sum_{i \in I_{j\tau}} \beta^{\tau-t} (p_{i\tau}^* - c_{i\tau}(E_{i\tau}; \theta^c)) q(\mathbf{p}_{\tau}^*, \mathbf{k}_{\tau})\right]$$
(16)

Replacing the cost function in equation (10) and applying the linear expectation operator, we obtain

$$V_j(s_t; s, \theta^c) = v_{0j} + \theta^c_{0j} v_{1j} + \theta^c_1 v_{2j} + \theta^c_2 v_{3j} + \theta^c_3 v_{4j}$$
(17)

Where

$$\begin{aligned} v_{0j} &= \sum_{\tau=t}^{\infty} \sum_{i \in I_{j\tau}} \beta^{\tau-t} E_t[q_i(\mathbf{p}^*_{\tau}, \mathbf{k}_{\tau})(p^*_{i\tau} - \varepsilon_{i\tau})] \\ v_{1j} &= -\sum_{\tau=t}^{\infty} \sum_{i \in I_{j\tau}} \beta^{\tau-t} E_t[q_i(\mathbf{p}^*_{\tau}, \mathbf{k}_{\tau})] \\ v_{2j} &= -\sum_{\tau=t}^{\infty} \sum_{i \in I_{j\tau}} \beta^{\tau-t} E_t[q_i(\mathbf{p}^*_{\tau}, \mathbf{k}_{\tau})DS_i] \\ v_{3j} &= -\sum_{\tau=t}^{\infty} \sum_{i \in I_{j\tau}} \beta^{\tau-t} E_t[q_i(\mathbf{p}^*_{\tau}, \mathbf{k}_{\tau})TR_i] \\ v_{4j} &= -\sum_{\tau=t}^{\infty} \sum_{i \in I_{j\tau}} \beta^{\tau-t} E_t[q_i(\mathbf{p}^*_{\tau}, \mathbf{k}_{\tau})\log(1 + E_{i\tau})] \end{aligned}$$

Notice that to obtain an estimate of these terms v for a given initial value of the state variables and a given path of random terms of the model, I only need to know the policy and demand functions, which were previously estimated. In the next subsection I explain the method used to obtain estimates of the terms in equation (17).

4.4 Simulation of the linear terms of the value function.

To estimate the dynamic cost parameters, the method uses the MPE constraints in (14), which require the evaluation of the value functions at observed choices as well as at one-step deviations from observed choices.⁷ BBL propose the use of Montecarlo integration over the random terms of the game to obtain an estimate of the linear terms v, which are then used to construct an estimate of the value function at any given value of the cost parameters. The Montecarlo procedure requires a forward simulation of the game, which is performed by taking random draws of the stochastic variables and calculating the average over the resulting discounted value of the linear terms for different sequences of draws. The same procedure is used to calculate the value function for the observed equilibrium policy and from small one-step deviations.

The computation of the EDV of the v terms is performed using the following algorithm:

- 1. Starting at a time t, at which a value for state s_0 is given, values for the corresponding random variables (the cost shock ε and the quality shocks α_f and α_o) are drawn from their corresponding distributions.
- 2. In the first period (time t) the observed price (or a deviation) is taken as the choice. For the following periods ($\tau > t$) the equilibrium price is predicted using the estimated policy function.
- 3. Given vectors of prices and quality, the demand for each available product is predicted and the terms v are updated accordingly. Using the law of motion for each state variable and the random draws, a new state for the next period, s_{t+1} , is determined.

⁷It suffices to assume that firms deviate in period t=0 and that they price using their policy functions in subsequent periods

4. In the following period, prices are predicted again given the new values of the state variables (s_{t+1}) . Steps (1) to (3) are repeated, and the values of the v terms are updated. I continue to update the value of the v terms for a large number of periods, until a time T in which β^T is small enough that the reminder of the infinite sum is approximately zero.

These steps generate a single path of the linear terms v in the expectation operator, given a single realization of the series of random shocks over time. To compute the expected value over those shocks a Montecarlo method is employed by repeating this procedure many times and taking the average over the results. For a given value of the unknown cost parameters, this procedure allows me to calculate the value function for the observed choice and also for deviations from the observed choice, so I am able to estimate the terms $\hat{V}_{jt}(\sigma_1(s), \sigma_2(s))$ and $\hat{V}_{jt}(\sigma'_1(s), \sigma_2(s))$ involved in equation (14). The EDV of the linear terms of the value function are used to estimate the unknown cost parameters as explained below.

4.5 Estimating the Dynamic Cost Parameters

Using the EDVs previously calculated, the BBL procedure constructs a loss function from the MPE constraint in equation (14). This equilibrium condition requires that, if a strategy profile is an MPE, then any one-step deviation, keeping the rival's strategy constant, must be unprofitable. This requirement is that for all j and all possible deviations $\sigma'_j(s)$:

$$V_j(\mathbf{s};\sigma_j(s),\sigma_{-j}(s);\theta^c) \ge V_j(\mathbf{s};\sigma'_j(s),\sigma_{-j}(s);\theta^c)$$

Define $g_j(\theta^c) \equiv V_j(\mathbf{s}; \sigma_j(s), \sigma_{-j}(s); \theta^c) - V_j(\mathbf{s}; \sigma'_j(s), \sigma_{-j}(s); \theta^c)$; then the previous condition can be written as

$$g_j(\theta^c) \ge 0 \tag{18}$$

Then for a given value of θ and a sample of size n we define a quadratic loss function based on the observations that violate that condition

$$Q(\theta^c|n) = \frac{1}{n} \sum_{j=1}^{2} \sum_{k=1}^{n} \left(\min\{g_j^k(\theta^c), 0\} \right)^2$$
(19)

Where k is an index for every observation in the sample. This quadratic function measures how far the observed behavior is from representing a Markov perfect equilibrium at a given value of θ . To bring the observed behavior as close as possible to an MPE I minimize the value of $Q_j(\theta^c|n)$. Therefore, the estimated value of the dynamic cost parameters is given by

$$\hat{\theta^c} = \operatorname*{argmin}_{\theta^c} Q(\theta^c | n)$$

5 Data and Results

The main data set was obtained from In-Stat/MDR, a research company that specializes in the CPU market⁸. It includes estimates of quarterly sales for CPUs aggregated into 29 product categories for the period 1993-2004 (48 quarters) and due to entry and exit of products over time I have a total of

⁸This dataset is proprietary material belonging to In-Stat/MDR.

291 observations⁹. The dataset also contains information on prices¹⁰. In-Stat obtains figures on list prices of Intel products and adjusts them for volume discounts offered to their major customers. Their main sources are the 10K Financial Statements reports and the World Semiconductor Trade Statistics elaborated by the Semiconductor Industry Association (SIA). They use this information to estimate unit shipments for each product by Intel and AMD, based on engineering relationships and the production capacity of each plant. The In-Stat/MDR data set is complemented with two other sources. The first is firm-level advertising expenditures. These data have been obtained from the 10K and 10Q financial statements. The second supplementary source consists of information about CPU performance from The CPU Scorecard, a company that measures on a comparative basis the performance of different CPU products. The In-Stat database has been previously used by Song (2006, 2007) to estimate consumer welfare in the CPU market and investment in research and development, and by Gordon (2008) to estimate a demand model for durable goods.

5.1 Demand estimation

The demand estimation method is presented in detail in Salgado (2008). Table 5 shows the results of the demand model that are used in the simulation of the dynamic model.

⁹An observation is one product in a given time period.

¹⁰In the In-Stat/MDR dataset, prices for AMD products are available only for the period 1999 to 2004. Therefore, the dataset was complemented with several other sources, including printed publications and on-line historical databases. Also, it contains 9 AMD CPUs and 20 Intel CPUs in the sample period.

Table 2: Results of Demand Estimation

Var.	Coeff.	St. Error	t-value	p-value
Price	19.6622	4.1766	4.7077	0.0000
Quality	5.8358	2.3671	2.4654	0.0195
Intel brand	3.3579	0.7899	4.2510	0.0000
σ_{price}	13.2787	3.1019	4.2808	0.0000
$\sigma_{quality}$	7.9928	3.0003	2.6640	0.0118
Average Price Elasticity	-2.43			

5.2 Evolution of Quality

The quality frontier was estimated using a logistic curve of the following form:

$$FK(t) = \kappa_0 \frac{1 + \kappa_1 exp(-\kappa_2 t)}{1 + \kappa_3 exp(-\kappa_2 t)}$$
(20)

The frontier was estimated as the envolvent of the observed quality data. To estimate it, I calculate the parameters of the logistic function that minimize the sum of the errors from the frontier to the observed data, constraining the errors to be positive. The estimated parameter are presented in table 3.

Parameter	Value
κ_0	11839
κ_1	7.4993
κ_2	0.1544
κ_3	321.1430

Table 3: Parameters of Quality Frontier

Recall that I assume that new products enter the market with quality $(1 - \alpha_n)FK(t)$ with $\alpha_n \sim \text{Uniform}[\underline{\alpha}_n, \overline{\alpha}_n]$. In the dataset I observe products that are introduced at a quality very close to the frontier and that are designated to compete in a high-performance segment; however, there

are also some products that are destinated to a value-segment and they are introduced at a quality significantly below the quality frontier. For this reason I differentiate between frontier products, for which $\alpha_n^f \sim U(\underline{\alpha}_n^f, \overline{\alpha}_n^f)$ and non-frontier products, for which $\alpha_n^{nf} \sim U(\underline{\alpha}_n^{nf}, \overline{\alpha}_n^{nf})$. In successive periods following the introduction of a product, its quality increases with probability p_o , which I assume is common between frontier and non-frontier products. If a product increases its quality, it does so in a proportion α_o , so that $k_t = (1 + \alpha_o)k_{t-1}$, with $log(\alpha_o) \sim N(\mu_o, \sigma_o^2)$. The estimated parameters are presented in Table 4.

 Table 4: Parameters of Quality Evolution

Parameter	Value
$(\underline{lpha}_n^f,\overline{lpha}_n^f)$	(0.00, 0.06)
$(\underline{lpha}_n^{nf},\overline{lpha}_n^{nf})$	(0.13, 0.71)
p_o	0.6770
μ_o	-2.8948
σ_o	0.7256

Figure 1 presents the observed evolution of quality of the products in the dataset and the estimated quality frontier. The individuals colored lines show the observed index of quality for a given product over its life and the doted blue line shows the estimated logistic quality frontier.

5.3 Policy function

I estimate the policy function using a quadratic polynomial approximation. Prices are predicted using profit-relevant state variables as explanatory varialbes. The variables used to predict product prices are the relative quality of the good compared to the quality of the best product available in the mar-



Figure 1: Evolution of Quality and Quality Frontier

ket (which enters the demand function) the production experience (which determines production costs) and the total experience of the competitor (which captures the effect of a firm' choices over the competitor response in the MPE). Figure 2 shows the observed and predicted prices using the estimated quadratic approximation to the policy function. The differences between observed and predicted are assumed to be the realized cost shocks.

5.4 Cost Parameters

I estimate two models of the cost function. In the first model I assume that the cost function is common to both firms. Firms face the same cost function, but they have different costs because they have products with different characteristics (die size and number of transistors) and different production



Figure 2: Policy Function

levels, and therefore are at different locations along the learning curve. In the second model, I incorporate a dummy variable for AMD to control for other potential cost differences between the two firms. The estimated cost parameters are presented in Table 5. All of the parameters are statistically significant at a 5% confidence level, except for the die size, which becomes insignificant in Model 2.

The Table 6 shows estimated average learning rates and average cost for each time period, for each firm, and for both cost models. Learning rates fluctuate between 2.54% and 24.86%. On average, Model 1 yields higher learning rates, with an average of 11.46% for AMD and 14.40% for Intel. Model 2 yields lower learning rates, with an average of 3.33% for AMD and 8.07% for Intel. Also, in Model 2 AMD's average costs is more than twice the average cost of Intel, while in Model 1 AMD's average cost is just 23.5%

Model 1							
Var.	Coeff. St. Error t-value p-va						
Constant	142.6800	11.8530	12.0375	0.0000			
Die Size	0.0758	0.0270	2.8027	0.0082			
Transistors	0.2564	0.0609	4.2118	0.0000			
Experience	10.7329	0.8126	13.2077	0.0000			
Model 2							
Var.	Coeff.	St. Error	t-value	p-value			
Constant	49.9756	0.9564	52.25	0.0000			
Die Size	0.0602	0.1390	0.43	0.3633			
Transistors	0.2607	0.0670	3.89	0.0002			
Experience	4.5174	0.4199	10.76	0.0000			
Dummy AMD	49.2492	0.3593	137.07	0.0000			

Table 5: Estimated Cost Parameters

higher than Intel's cost. The differences in cost between firms in Model 2 are explained mostly (88%) by the constant term and the remaining 12% is explained by lower learning due to lower production volumes by AMD.

6 Conclusions

In this paper I have estimated a dynamic cost function with learning-bydoing in the PC CPU industry. The results shows that there exists important differences in firms' estimated production costs, with AMD's average costs being more than twice Intel's average costs in a model in which the cost function is allowed to differ between firms. These differences in production costs are explained by both higher production costs when products are introduced, as well as lower learning due to lower production volumes by AMD. The average estimated learning rates fluctuate between 2.18% and 22.01%. These rates are lower when compared to previous studies for other semicon-

Learning RatesProduction CostsLearning RatesProduction CostsQuarterAMDINTELAMDINTELAMDINTEL1 5.00% 4.99% 148.89 149.06 2.72% 4.74% 115.14 66.1 2 10.93% 5.37% 68.06 138.44 3.66% 4.98% 85.6 62.84 3 10.12% 11.27% 73.51 66.03 3.57% 8.70% 87.62 35.99 4 9.21% 12.98% 80.77 57.32 3.47% 9.39% 90.31 33.35 5 9.82% 12.83% 75.79 58 3.54% 9.44% 88.51 33.36 6 10.75% 12.06% 69.21 59.06 3.87% 7.50% 82.9 41.77 9 13.22% 11.99% 56.28 62.05 3.85% 7.75% 81.39 40.4 10 14.44% 11.78% 52.99 63.14 3.90% 8.65% 79.21 36.2 11 14.9% 12.64% 50.29 58.44 3.95% 8.65% 77.33 36.16 11 14.9% 13.89% 44.389 40.7% 9.90% 7.33 36.61 15 16.91% 14.33% 45.08 51.91 4.05% 8.66% 77.33 36.61 16 17.11% 13.87% 43.48 53.97 4.07% 9.90% 76.99 31.64 16 17.11% 15.5% 14.37% <th></th> <th colspan="3">Model 1</th> <th colspan="4">Model 2</th>		Model 1			Model 2				
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		Learnin	g Rates	Proudue	ction Costs	Learnii	ng Rates	Proudue	ction Costs
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	Quarter	AMD	INTEL	AMD	INTEL	AMD	INTEL	AMD	INTEL
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	1	5.00%	4.99%	148.89	149.06	2.72%	4.74%	115.14	66.1
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	2	10.93%	5.37%	68.06	138.44	3.66%	4.98%	85.6	62.84
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	3	10.12%	11.27%	73.51	66.03	3.57%	8.70%	87.62	35.99
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	4	9.21%	12.98%	80.77	57.32	3.47%	9.39%	90.31	33.35
	5	9.82%	12.83%	75.79	58	3.54%	9.44%	88.5	33.16
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	6	10.75%	12.60%	69.21	59.05	3.64%	8.51%	86.1	36.77
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	7	11.70%	12.54%	63.58	59.34	3.73%	8.17%	84.05	38.31
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	8	12.32%	11.59%	60.4	64.2	3.78%	7.50%	82.9	41.77
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	9	13.22%	11.99%	56.28	62.05	3.85%	7.75%	81.39	40.4
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	10	14.04%	11.78%	52.99	63.14	3.90%	8.26%	80.19	37.89
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	11	14.79%	12.64%	50.29	58.84	3.95%	8.65%	79.21	36.2
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	12	15.40%	13.69%	48.3	54.36	3.99%	9.06%	78.48	34.55
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	13	16.01%	14.03%	46.46	53.02	4.02%	9.22%	77.81	33.98
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	14	16.50%	14.33%	45.08	51.91	4.05%	8.66%	77.33	36.16
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	15	16.91%	16.95%	44	43.89	4.07%	9.90%	76.99	31.64
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	16	17.11%	13.78%	43.48	53.97	4.07%	8.50%	76.94	36.82
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	17	9.73%	12.87%	76.46	57.8	3.29%	7.35%	95.06	42.6
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	18	5.71%	11.54%	130.27	64.45	2.54%	6.63%	123.28	47.21
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	19	7.91%	10.84%	94	68.63	2.84%	5.62%	110.21	55.69
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	20	9.33%	10.27%	79.77	72.42	2.98%	5.37%	105.01	58.29
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	21	10.36%	9.35%	71.79	79.57	3.07%	6.21%	102.09	50.44
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	22	10.83%	11.82%	68.69	62.94	3.11%	7.11%	100.84	44.04
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	23	8.88%	14.40%	83.82	51.65	3.13%	7.81%	100.14	40.09
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	24	11.22%	17.27%	66.3	43.07	3.37%	8.53%	92.97	36.72
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	25	13.10%	13.80%	56.8	53.91	3.51%	7.71%	89.32	40.63
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	26	13.42%	14.65%	55.44	50.78	3.52%	7.94%	88.86	39.46
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	27	6.76%	14.74%	110.02	50.48	2.77%	7.96%	113.02	39.33
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	28	9.61%	10.26%	77.38	72.5	3.12%	6.79%	100.27	46.09
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	29	9.59%	13.62%	77.56	54.6	3.08%	8.68%	101.65	36.06
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	30	10.24%	17.68%	72.62	42.07	3.13%	9.98%	100.12	31.36
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	31	10.95%	21.74%	67.94	34.23	3.18%	10.99%	98.4	28.48
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	32	11.73%	24.86%	63.45	29.93	3.24%	11.61%	96.6	26.98
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	33	12.04%	22.64%	61.77	32.86	3.25%	10.41%	96.3	30.08
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	34	12.08%	24.41%	61.59	30.48	3.24%	10.58%	96.6	29.61
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	35	12.78%	20.97%	58.23	35.47	3.32%	9.87%	94.18	31.73
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	36	13.39%	21.28%	55.58	34.95	3.37%	10.04%	93	31.2
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	37	13.85%	15.35%	53.7	48.46	3.37%	8.76%	92.89	35.72
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	38	14.28%	11.72%	52.09	63.47	3.37%	7.22%	92.92	43.4
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	39	14.46%	15.08%	51.44	49.34	3.36%	8.24%	93.13	38.01
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	40	14.63%	14.37%	50.87	51.79	3.36%	7.16%	93.09	43.73
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	41	15.07%	16.17%	49.36	46	3.39%	7.53%	92.4	41.58
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	42	14.73%	16.97%	50.51	43.84	3.37%	7.30%	92.99	42.89
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	43	9.30%	18.09%	80.02	41.13	2.93%	7.32%	106.96	42.77
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	44	7.48%	19.35%	99.49	38.44	2.67%	7.47%	117.39	41.92
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	45	7.35%	13.84%	101.28	53.74	2.62%	6.70%	119.55	46.73
47 8.81% 12.16% 84.43 61.17 2.77% 6.89% 113 45.47	46	7.85%	11.55%	94.82	64.4	2.66%	6.55%	117.64	47.82
	47	8.81%	12.16%	84.43	61.17	2.77%	6.89%	113	45.47
48 8.62% 13.98% 86.33 53.23 2.73% 7.49% 114.8 41.82	48	8.62%	13.98%	86.33	53.23	2.73%	7.49%	114.8	41.82
Min 5.00% 4.99% 43.48 29.93 2.54% 4.74% 76.94 26.98	Min	5.00%	4.99%	43.48	29.93	2.54%	4.74%	76.94	26.98
Average 11.46% 14.40% 70.23 56.88 3.33% 8.07% 95.69 40.29	Average	11.46%	14.40%	70.23	56.88	3.33%	8.07%	95.69	40.29
Max 17.11% 24.86% 148.89 149.06 4.07% 11.61% 123.28 66.1	Max	17.11%	24.86%	148.89	149.06	4.07%	11.61%	123.28	66.1

 Table 6: Average Learning Rates and Production Costs by Firm

ductor products that have found average learning rates around 20%. This is an indication that firms are more successful in transfering the products from the development to fabrication facilities and have already advanced in their learning curve when the products are introduced into the market. Nevertheless, given the importance of CPU products for the industry this result is not surprising.

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